

# On Faults and Faulty Programs

**Ali Jaoua, Marcelo Frias, Ali Mili**

**RAMICS 2014**

**Marienstatt im Westerwald, Apr/May 2014**

# Outline

- **What's Wrong with Faults**
- **Correctness and Relative Correctness**
- **Faults and Monotonic Fault Removal**
- **Definite Faults**
- **Beyond Nice Definitions: Applications**
- **Conclusion**

# What's Wrong with Faults

2004: Avizienis, Laprie, Randell, Landwehr

- Terminology for dependability
  - Fault (attribute of a product that precludes its correct behavior).
  - Error (state of the program produced by sensitization of the fault).
  - Failure (violation of the system specification pursuant the sensitization of a fault).
- Failure
  - Well defined property, with respect to a well defined specification

# What's Wrong with Faults

Many issues with defining faults:

- Characterization of a fault dependent on implicit design:
  - Has no official existence.
  - Is not documented/ validated/ vetted.
  - Gap between designer's intent, tester's understanding of the intent.
  - Contingent upon implicit assumptions about other parts of the product.

# What's Wrong with Faults

The same failure may be blamed on many fault configurations:

- Neither the location,
- Nor the number,
- Nor the nature of the fault is determined
  - Wrong operator,
  - Wrong operand,
  - Wrong condition,
  - Missing path.
- What does it mean to remove the fault?
  - It certainly does not mean that now the program is correct, since it may still have other faults.
  - We are lucky if we did not make it worst.

# What's Wrong with Faults

Specification:  $R = \{(x, x') \mid x' = x^2 \bmod 5\}$ .

```
{read(x); x=x*2; x=x%5; write(x);}
```

```
{read(x); x=x*2; x=x%5; write(x);}
```

```
{read(x); x=x*2; x=((x/2)**2)%5; write(x);}
```

```
{read(x); x=x*2; x=((x/2)**2); x=x%5; write(x);}
```

```
{read(x); x=x*2; x=x*x; x=(x/4)%5; write(x);}
```

# What's Wrong with Faults

This casts a shadow on such concepts as

- Fault density,
- Fault proneness,
- Estimates of the number of faults.

If the same failure can be remedied by changing one statement or two statements,

- Does that count as one fault or two faults,

If a missing path is remedied by adding a new path of 20 lines,

- how many faults is that?

# Outline

- **What's Wrong with Faults**
- **Correctness and Relative Correctness**
- **Faults and Monotonic Fault Removal**
- **Definite Faults**
- **Beyond Nice Definitions: Applications**
- **Conclusion**

# Correctness and Relative Correctness

## Program functions

```

#include <iostream> ... .. line 1
void count (char q[]) {int let, dig, other, i, l; char c; 2
    i=0; let=0; dig=0; other=0; l=strlen(q); // body init 3
    while (i<l) { // cond t 4
        c = q[i]; // body b0 5
        if ('A'<=c && 'Z'>c) let+=2; // cond c1, body b1 6
        else 7
        if ('a'<=c && 'z'>=c) let+=1; // cond c2, body b2 8
        else 9
        if ('0'<=c && '9'>=c) dig+=1; // cond c3, body b3 10
        else 11
            other+=1; // body b4 12
        i++;} // body inc 13
    printf ("%d %d %d\n", let, dig, other);} // body p 14

```

# Correctness and Relative Correctness

## Program functions

$$COUNT = INIT \circ ((T \cap B)^* \cap \widehat{T}) \circ P.$$

$$B = B0 \circ NEST \circ INC,$$

$$NEST = (C1 \cap B1) \cup \overline{C1} \cap ((C2 \cap B2) \cup \overline{C2} \cap ((C3 \cap B3) \cup \overline{C3} \cap B4)).$$

**Granularity determines precision of fault diagnosis.**

# Correctness and Relative Correctness

## Refinement, Correctness

**Definition 2.1.** Refinement, due to [BEM92]. Let  $R$  and  $R'$  be two relations on set  $S$ . We say that  $R$  refines relation  $R'$  (and we write:  $R \sqsupseteq R'$ ) if and only if:  $RL \cap R'L \cap (R \cup R') = R'$ .

Program  $g$  is correct with respect to  $R$  iff  $G$  refines  $R$ .

Program  $g$  is correct with respect to  $R$  iff  $dom(R \cap G) = dom(R)$ .

# Correctness and Relative Correctness

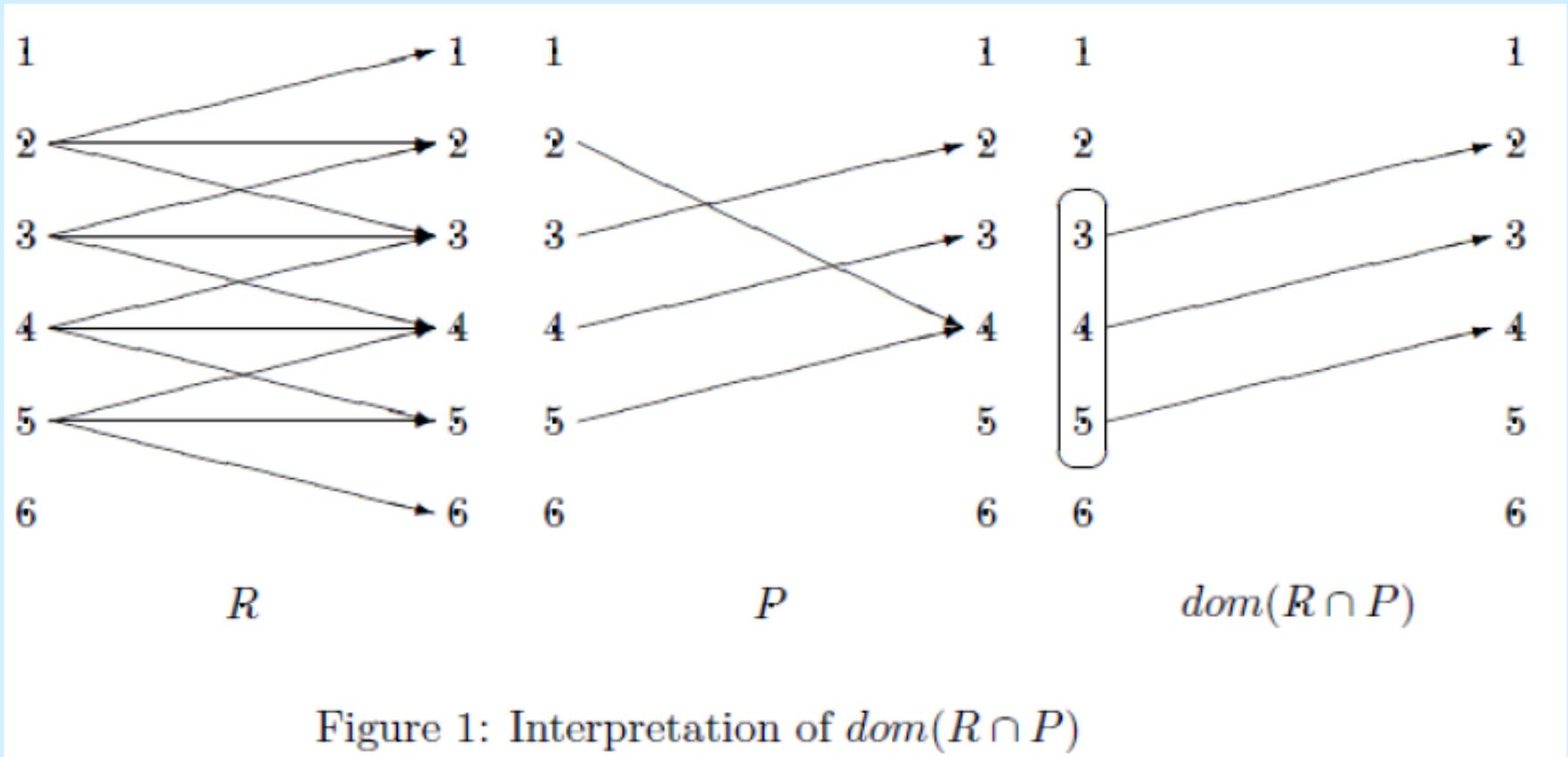


Figure 1: Interpretation of  $dom(R \cap P)$

# Correctness and Relative Correctness

## Relative Correctness

**Definition 2.4. Relative Correctness.** *Given a relation  $R$  on space  $S$  and two programs  $g$  and  $g'$  on space  $S$ , we say that  $g$  is more-correct than  $g'$  with respect to  $R$  if and only if*

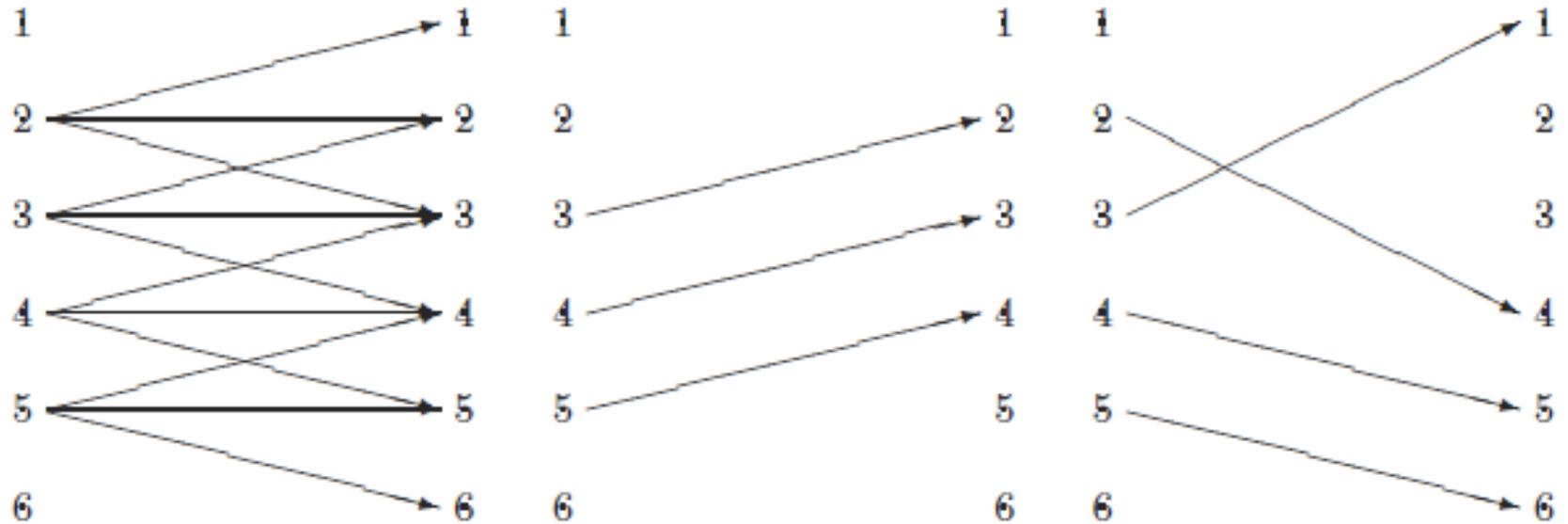
$$(G \cap R)L \supseteq (G' \cap R)L.$$

*Also, we say that  $g$  is strictly-more-correct than  $g'$  with respect to  $R$  if and only if*

$$(G \cap R)L \supset (G' \cap R)L.$$

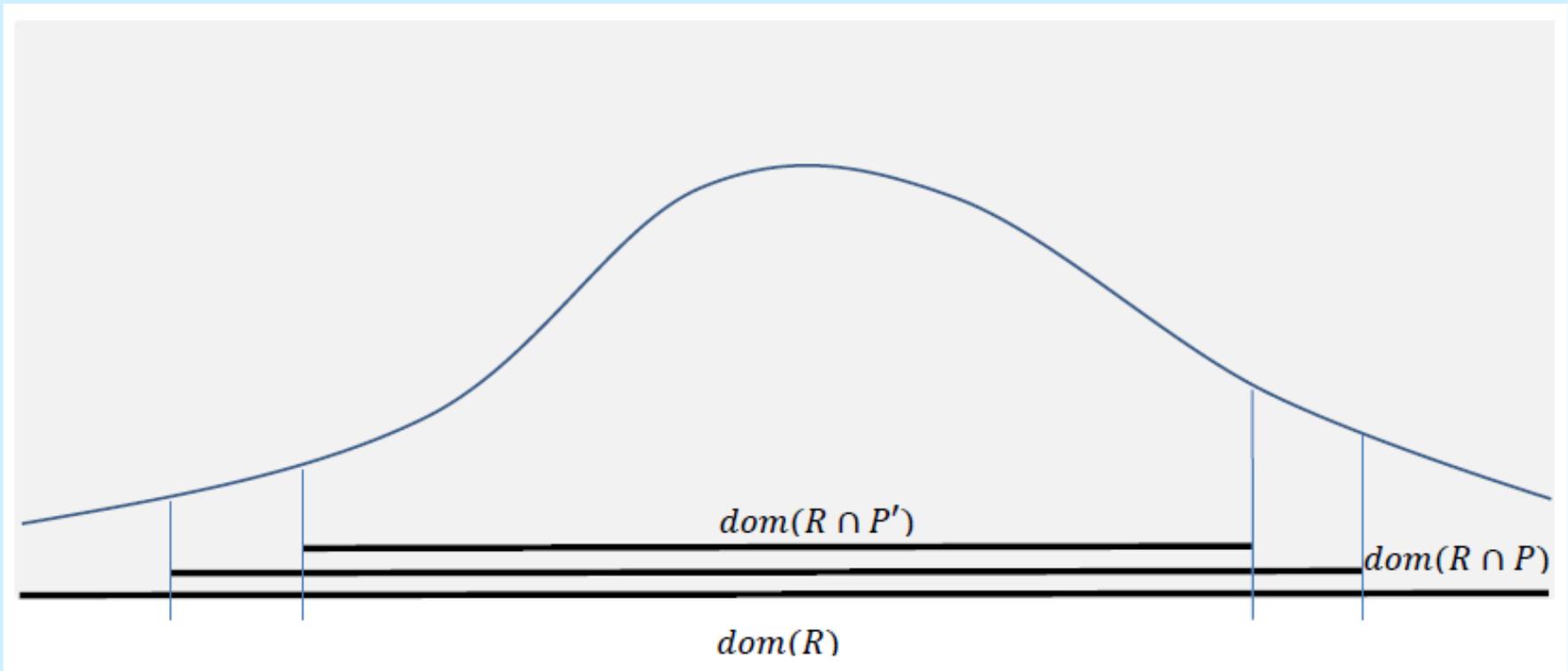
# Correctness and Relative Correctness

Relative Correctness does not mean preserving correct behavior:



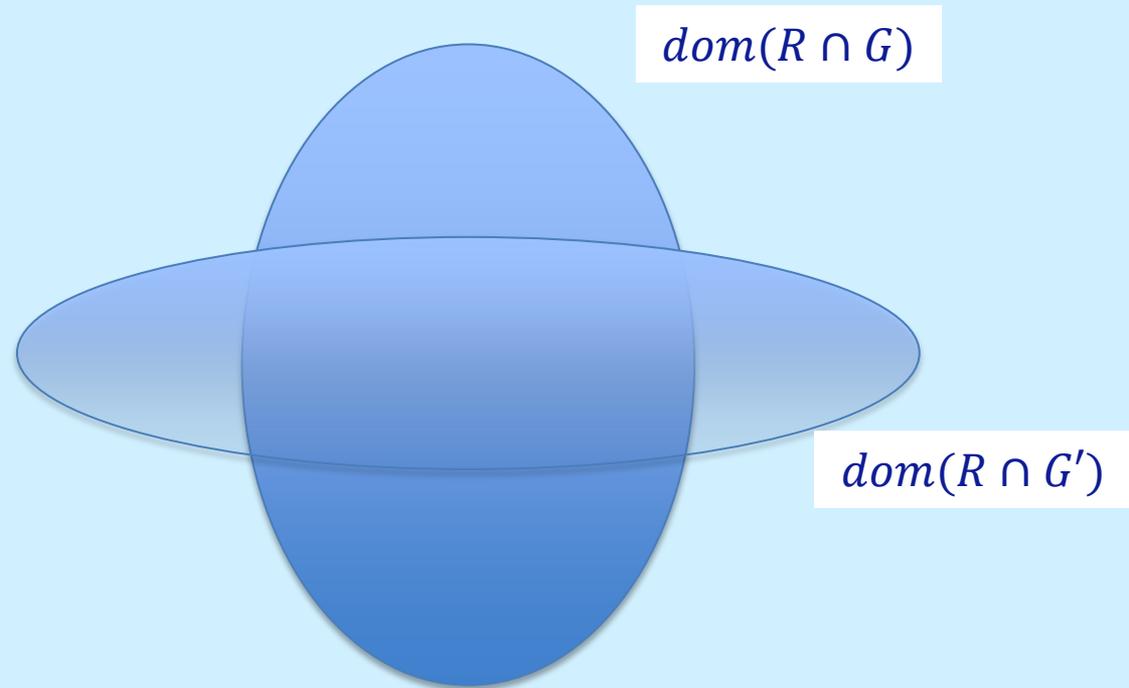
# Correctness and Relative Correctness

## Relative Correctness and Reliability



# Correctness and Relative Correctness

A program may be more reliable w/o being more-correct.



# Correctness and Relative Correctness

## Quantifying Relative Correctness

- $\forall G': (R \cap G)L \supseteq (R \cap G')L.$

—

- $\forall R: (R \cap G)L \supseteq (R \cap G')L.$

—

# Correctness and Relative Correctness

## Quantifying Relative Correctness

- $\forall G': (R \cap G)L \supseteq (R \cap G')L.$ 
  - $G$  is correct with respect to  $R$ .
- $\forall R: (R \cap G)L \supseteq (R \cap G')L.$ 
  - $G$  refines  $G'$ .

# Outline

- What's Wrong with Faults
- Correctness and Relative Correctness
- **Faults and Monotonic Fault Removal**
- Definite Faults
- Beyond Nice Definitions: Applications
- Conclusion

# Faults and Monotonic Fault Removal

**Definition 3.1. Contingent Faults.** *Let  $g$  be a program on space  $S$ , and let  $\theta(G_1, G_2, G_3, \dots, G_n)$  be a relational representation of program  $g$  at a given level of granularity. We say that  $G_i$  is a fault of program  $g$  with respect to specification  $R$  if and only if there exists a relation  $G'_i$  on  $S$  such that  $\theta(G_1, G_2, G_3, \dots, G'_i, \dots, G_n)$  is strictly-more-correct with respect to  $R$  than  $\theta(G_1, G_2, G_3, \dots, G_i, \dots, G_n)$ .*

**Contingent fault:** contingent upon the hypothesis that we are focusing the blame on  $G_i$ .

We may have to broaden it to include any number of fault loci.

# Faults and Monotonic Fault Removal

**Definition 3.2. Monotonic Fault Removal.** *Let  $g$  be a program on space  $S$ , whose expression is  $\theta(G_1, G_2, G_3, \dots, G_i, \dots, G_n)$  and let  $G_i$  be a contingent fault in  $g$ . We say that the substitution of  $G_i$  by  $G'_i$  is a monotonic fault removal if and only if program  $g'$  defined by  $\theta(G_1, G_2, G_3, \dots, G'_i, \dots, G_n)$  is strictly-more-correct than  $g$ .*

*To be a fault: Unary property.*

*To be a monotonic fault removal: binary property (faulty statement and its replacement).*

# Faults and Monotonic Fault Removal

In the same way that program construction proceeds, ideally, by stepwise refinement,

$$R \bar{\subseteq} R_1 \bar{\subseteq} R_2 \bar{\subseteq} R_3 \bar{\subseteq} R_4 \bar{\subseteq} \dots g.$$

Program testing ought to proceed, ideally, by stepwise monotonic fault removal.

$$g \bar{\subseteq} g_1 \bar{\subseteq} g_2 \bar{\subseteq} g_3 \bar{\subseteq} g_4 \bar{\subseteq} \dots g.$$

# Faults and Monotonic Fault Removal

## Illustration:

- $g_{01}$  The program obtained from  $g$  when we replace  $(\text{let}+=2)$  by  $(\text{let}+=1)$ .
- $g_{10}$  The program obtained from  $g$  when we replace  $(\text{'Z'}>c)$  by  $(\text{'Z'}>=c)$ .
- $g_{11}$  The program obtained from  $g$  when we replace  $(\text{let}+=2)$  by  $(\text{let}+=1)$   $(\text{'Z'}>c)$  by  $(\text{'Z'}>=c)$ .

$$\begin{aligned} - (R_0 \cap G)L &= \{(s, s') | q \in \text{list}\langle \alpha_a \cup \nu \cup \sigma \rangle\}. \\ - (R_0 \cap G_{01})L &= \{(s, s') | q \in \text{list}\langle (\alpha_A \setminus \{\text{'Z'}\}) \cup \alpha_a \cup \nu \cup \sigma \rangle\}. \end{aligned}$$

$$\begin{aligned} - (R_0 \cap G_{10})L &= \{(s, s') | q \in \text{list}\langle \alpha_a \cup \nu \cup \sigma \rangle\}. \\ - (R_0 \cap G_{11})L &= \{(s, s') | q \in \text{list}\langle \alpha_A \cup \alpha_a \cup \nu \cup \sigma \rangle\}. \end{aligned}$$

# Faults and Monotonic Fault Removal

## Illustration:

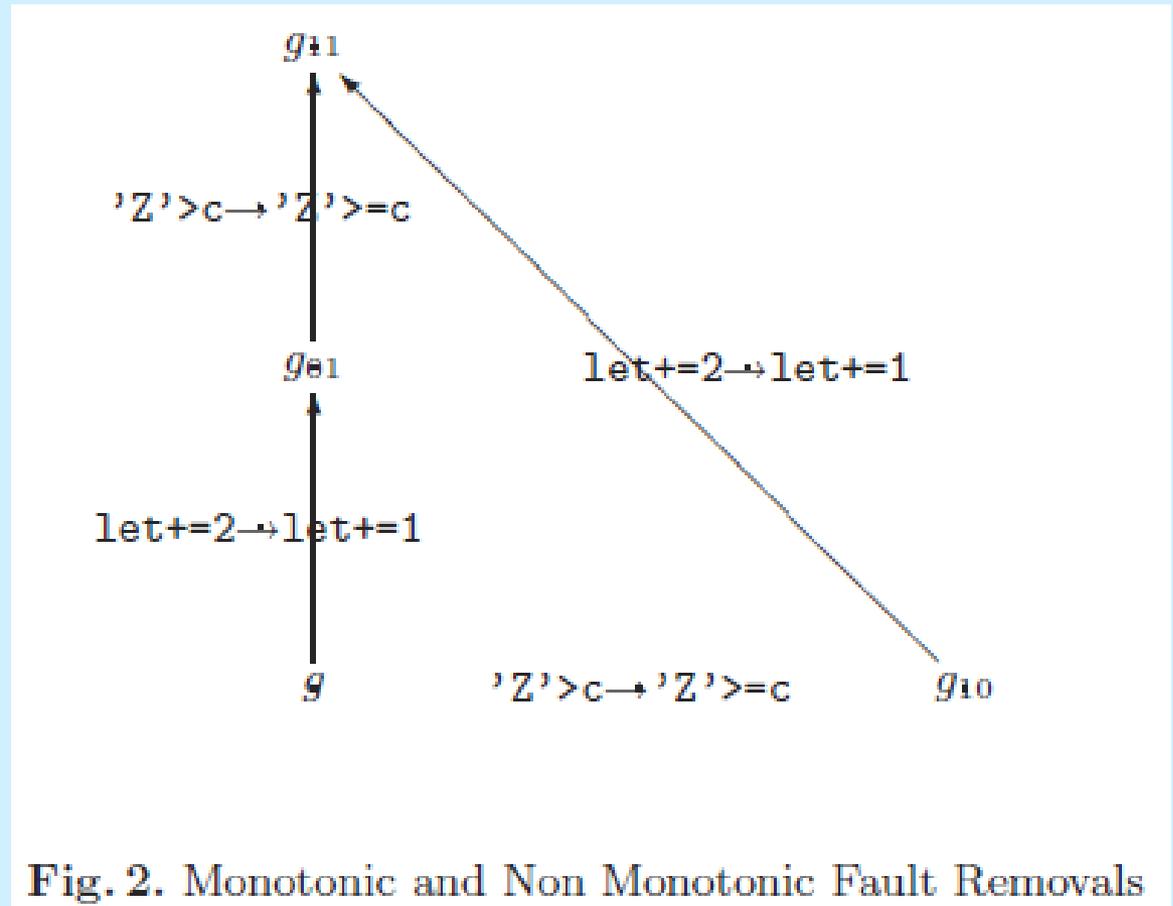


Fig. 2. Monotonic and Non Monotonic Fault Removals

# Faults and Monotonic Fault Removal

Does every fault removal have to be monotonic (produce a more-correct program?)

- Yes.

What about the transformation of  $g$  into  $g_{10}$ ?

- We broaden the definition of fault to include more than one location (other reasons to do so, anyway) and we view the transition  $(g, g_{10}, g_{11})$  as a single fault removal.

# Outline

- What's Wrong with Faults
- Correctness and Relative Correctness
- Faults and Monotonic Fault Removal
- **Definite Faults**
- Beyond Nice Definitions: Applications
- Conclusion

# Definite Faults

**Not all faults are contingent.**

- **Some faults are so damaging that no amount of mitigation can salvage them.**
- **Examples:**
  - **Loss of injectivity in preprocessing.**
  - **Loss of surjectivity in postprocessing.**

# Definite Faults

## Loss of Injectivity.

**Lemma 4.2. Right Divisibility.** *The relational equation in  $X$ :  $QX \sqsupseteq R$ , admits a solution in  $X$  if and only if  $R$  and  $Q$  satisfy the following condition:*

$$RL \subseteq QL \wedge \overline{\widehat{Q}(R \cap RL)}L = L .$$

**Proposition 4.3. Definite Fault, for loss of injectivity.** *We consider a relation  $R$  on space  $S$  and a program  $g$  on  $S$  of the form  $g = \{g_1; g_2\}$ . If  $R$  and  $G_1$  do not satisfy the right divisibility condition (with  $G_1$  as  $Q$ ), then  $g_1$  is definitely faulty with respect to  $R$ .*

# Definite Faults

**Loss of Injectivity.**

**Specification:**

- **Sorting an array:**
  - **Preprocessing: destroy one cell.**
  - **Nothing that post-processing can do recover from the loss.**

# Definite Faults

## Loss of Surjectivity

**Lemma 4.4.** *Left Divisibility.* The relational equation in  $X$ :  $XQ \sqsupseteq R$ ,  $\hat{X}L \subseteq QL$ , admits a solution in  $X$  if and only if  $R$  and  $Q$  satisfy the following condition:

$$RL \subseteq (\overline{R\hat{Q}} \cap L\hat{Q})L .$$

**Proposition 4.5.** *Definite Fault, for loss of surjectivity.* We consider a relation  $R$  on space  $S$  and a program  $g$  on  $S$  of the form  $g = \{g_1; g_2\}$ . If  $R$  and  $G_2$  do not satisfy the right divisibility condition (with  $G_2$  as  $Q$ ), then  $g_2$  is definitely faulty with respect to  $R$ .

# Definite Faults

## Loss of Surjectivity

- Specification:

$$R = \{(s, s') \mid s' = s^2 \text{ mod } 6\} .$$

- Post processing:

$$g_2 = \{s = s \text{ mod } 3\}$$

- No preprocessor can make up for this fault.

# Outline

- What's Wrong with Faults
- Correctness and Relative Correctness
- Faults and Monotonic Fault Removal
- Definite Faults
- **Beyond Nice Definitions: Applications**
- Conclusion

# Beyond Nice Definitions: Applications

We have lived happily for several decades without a definition of faults.

- We can live happily everafter...
- Why do we need a definition?

Applications:

- Streamline fault repair

# Beyond Nice Definitions: Applications

## Mutation Testing for Fault Repair

- Faults are within the range of mutation operators.
- Fault bound to one location.
- Realistic faults can be removed efficiently.
- The structure of the program is not in question.
- If a program passes the test, it is correct (fault removal confirmed).
- If a program fails the test, it is incorrect (fault removal should be rolled back).

# Beyond Nice Definitions: Applications

All hypotheses highly questionable:

- Faults are within the range of mutation operators.
  - **Good luck.**
- Fault bound to one location. The structure of the program is not in question.
  - **Limited scope.**
- Realistic faults can be removed efficiently.
  - **Painful dilemmas: realistic faults vs efficient fault removal.**
- If a program passes the test, it is correct (fault removal confirmed).
  - **May work on T but fail outside.**
- If a program fails the test, it is incorrect (fault removal should be rolled back).
  - **Does not have to be correct; only more-correct than original; not the last fault.**

## Beyond Nice Definitions: Applications

Specification  $R$ , faulty program  $g$ , candidate mutant  $g'$ .

- Is  $g'$  a legitimate improvement over  $g$ ?
  - Compare  $dom(R \cap G)$  and  $dom(R \cap G')$ .
- If modification buried inside a loop, it is difficult to compute  $G$  and  $G'$ .

# Beyond Nice Definitions: Applications

## Possible approach:

- Using invariant relations.
- Invariant relation of while t {b}:
  - Reflexive transitive superset of  $(T \cap B)$
- Can be used to prove
  - Correctness,
  - Incorrectnessof while loop with respect to specification  $V$ .

# Beyond Nice Definitions: Applications

```
// input: specification V
// output: correctness diagnosis; incompatible InvRel.
cumulR=L; diagnosis=undecided;
While (diagnosis=undecided && moreInvRel)
  {R = nextInvRel();
   CumulR = CumulR  $\cap$  R.
   if subsume(CumulR, V) {diagnosis = correct;}
   else
     if incompatible(R, V) {diagnosis = incorrect; return R;}
  }
// if (diagnosis=undecided) we ran out of invariant relations.
```

# Beyond Nice Definitions: Applications

## Three outcomes

- **Diagnosis = correct:**
  - No fault to remove.
- **Diagnosis = incorrect:**
  - Invariant Relation culprit. Used to calculate monotonic correction (statements, variables, ).
- **Diagnosis = undecided:**
  - Grow the database of Recognizers.

# Outline

- **What's Wrong with Faults**
- **Correctness and Relative Correctness**
- **Faults and Monotonic Fault Removal**
- **Definite Faults**
- **Beyond Nice Definitions: Applications**
- **Conclusion**

# Conclusion

Defined relative correctness, tripartite relation between a specification and two programs:

- Quantified over specifications: refinement.
  - Relative correctness: point-wise refinement.
- Quantified over programs: correctness.

Used relative correctness to define

- Contingent fault.
- Monotonic fault removal.
- Definite fault.

Explored some possible applications behind

- Nice looking definitions.

Infancy; envision to continue exploration.